

H.T. Banks

An Introduction to Statistical Methodology in Inverse Problems

Outline of Lectures

1. Introduction to statistical models and probability review
2. Statistical models and inference: asymptotic sampling distributions
3. Inverse problem methodology summary
 - (i) Parameter estimation (MLE, OLS, GLS), standard errors and confidence intervals
 - (ii) Model comparison techniques and significance tests for improvements in models

References

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